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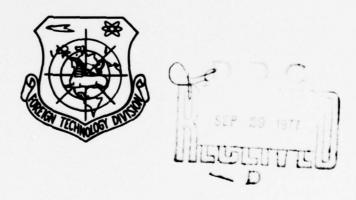




TRANSITION PROCESSES DURING COMPRESSION OF CYLINDRICAL SHELLS IN A STRONG MAGNETIC FIELD

Ву

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A a	A a	A, a	Pp	Pp	R, r
Бб	5 6	B, b	Сс	Cc	S, s
Вв	B .	V, v	Тт	T m	T, t
Гг	Γ:	G, g	Уу	уу	U, u
Дд	Дд	D, d	ФФ	<b>Ø Ø</b>	F, f
Еe	E .	Ye, ye; E, e*	X ×	X x	Kh, kh
жж	ж ж	Zh, zh	44	4 4	Ts, ts
3 э	3 ,	Z, z	4 4	4 4	Ch, ch
Ии	н и	I, i	Шш	Шш	Sh, sh
Йй	A a	У, у	Щщ	Щщ	Sheh, sheh
Н н	KK	K, k	Ъъ	<b>3</b> 8	11
Лл	ЛА	L, 1	Ыы	M W	Y, y
ММ	Мм	M, m	Ьь	ь.	•
Нн	Н н	N, n	Ээ	9 ,	Е, е
0 0	0 0	0, 0	Юю	10 m	Yu, yu
Пп	Пп	P, p	Яя	Яя	Ya, ya

<sup>\*</sup>ye initially, after vowels, and after b, b; e elsewhere. When written as ë in Russian, transliterate as yë or ë. The use of diacritical marks is preferred, but such marks may be omitted when expediency dictates.

#### GREEK ALPHABET

Alpha	Α	α	•		Nu	N	ν	
Beta	В	β			Xi	Ξ	ξ	
Gamma	Γ	Υ			Omicron	0	0	
Delta	Δ	δ			Pi	Π	π	
Epsilon	E	ε	ŧ		Rho	P	ρ	•
Zeta	Z	ζ			Sigma	Σ	σ	ς
Eta	Н	η			Tau	T	τ	
Theta	Θ	θ	\$		Upsilon	T	υ	
Iota	I	ι			Phi	Φ	φ	φ
Kappa	K	n	κ	×	Chi	X	χ	
Lambda	٨	λ			Psi	Ψ	Ψ	
Mu	М	и			Omega	Ω	ω	

### RUSSIAN AND ENGLISH TRIGONOMETRIC FUNCTIONS

Rus	sian	English
sin		sin
cos		cos
tg		tan
ctg		cot
sec		sec
cos	ec	csc
sh		sinh
ch		cosh
th		tanh
cth		coth
sch		sech
csc	h	csch
arc	sin	sin-1
arc	cos	cos-1
arc	tg	tan-1
arc	ctg	cot-1
arc	sec	sec-1
arc	cosec	csc <sup>-1</sup>
arc	sh	sinh <sup>-1</sup>
arc	ch	cosh-1
arc	th	tanh-1
arc	cth	coth <sup>-1</sup>
arc	sch	sech-1
arc	csch	csch <sup>-1</sup>
rot		curl
lg		log

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TRANSITION PROCESSES DURING COMPRESSION OF CYLINDRICAL SHELLS IN A STRONG MAGNETIC FIELD

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Leningrad Order of Lenin Polytechnical Institute imeni M. I. Kalinina

The compression of thin-walled metallic cylinders in a strong pulsed magnetic field is of interest in respect to the study of the behavior of metals under conditions of rapid deformations, observed during the magnetic-pulsed working of metals [1], with the obtaining of a strong magnetic field by means of flux compression [2]. There is independent significance in the question of the conversion of the energy of a magnetic field into the kinetic energy of an accelerated cylinder [3, 4].

FTD-ID(RS)I-1874-76

At the TVN [exPanSion not Verified] department of the LPI imeni M. I. Kalinina an experimental investigation was made of the deformation of metallic cylinders in a strong magnetic field, created during the discharge of a capacitor bank with a capacitance C=12.8 μP with a stored energy W<sub>0</sub>=92 kJ (with a charge voltage U<sub>0</sub>=120 kV) through a matching transformer on a signle-turn solenoid (Pigure 1). In the tests the change in the radius of cylinders which were arranged coaxally inside of a solenoid Was recorded, and oscillograms were made of the magnetic induction inside and outside of the cylinder.

Calculations of the movement of a deformed cylinder without taking into account such factors as the penetration of the field inside of the cylinder, its heating up by vertex currents, and redistribution of current over the surface of the solenoid during deformation give results which differ significantly from experimental data [3]. The purpose of the present work is a more stringent description of the process of compression, taking into account the listed features of the deformation of a cylinder in the field of a single-turn solenoid.

In the derivation of equations the magnetic field in the working

gap between the solenoid and cylinder  $B_c$  is considered uniform. This is valid in the beginning of the process of acceleration of the cylinder, while the working gap is small. With deep compression the field differs from uniform, but on this stage the influence of the external field on the movement of the cylinder is not great. The field inside of the shell is also accepted as uniform, this field has a noticeable influence on movement only on the final sector of compression, when the supposition of its uniformity is fulfilled. Under these conditions the equation of purely inertial movement of the cylinder we write in the form

(1) 
$$m \frac{d^2R}{dl^2} = \frac{1}{2\mu_0} (B_e^2 - B_i^2) 2\pi R l,$$

where R - current radius of the deformed part of the cylinder;

7 - its axial length;

m - its mass.

The assumptions made also lead to the following formulas for the inductance of the working gap:

(2) 
$$L_2 = \frac{\mu_c \pi}{I} (R_c^2 - R^2),$$

FTD-ID(RS)I-1874-76

where  $R_c$  - radius of the solenoid, and the inductance of the deformed part of the cylinder

$$(3) L_3 = \frac{\mu_0 \pi}{l} R^2.$$

Since the process of compression lasts all told only several tens of microseconds, then it is possible to disregard the heat exchange between the cylinder and the surrounding medium and to write for its heat content q<sub>3</sub> the equation

$$\frac{dq_3}{dt}=i_3^2r_{30}\left(1+\frac{\alpha q_3}{c}\right)\left(\frac{R}{R_0}\right)^2,$$

in which the change in the active resistance of the cylinder  $r_3$  is taken into account in the case of compression due to heating and a change in the thickness of the wall during deformation.

In equation (4) i<sub>3</sub> - vortex current in the cylinder;  $r_{30}$  and  $P_0$  - initial values of active resistance and the radius of the cylinder;  $\alpha$  - temperature coefficient of resistance; c - heat capacity of the cylinder.

A special feature of the single-turn sclenoid is the fact that part of its current flows over the end surfaces and does not take

part in the creation of the working field, which is determined by the current which is flowing over the cylindrical surface of the solenoid. In the process of deformation the relationship between the indicated parts of the overall Current of the solenoid is changed. This circumstance is taken into account by the approximation formula of equivalent inductance of the solenoid-cylinder system [5]

(5) 
$$L = \frac{2\pi\mu_0 R_c h}{l + \frac{4h}{\pi} \left(1,46 + \ln \frac{\pi R_c}{4h}\right)},$$

where  $h=R_c-R$ . - the gap between the sclenoid and the cylinder. In the derivation of (5) it is considered that  $h \ll R_c$ , and the system operates under conditions of a sharp surface effect.

Pormula (5) can be presented in the form

$$L=\frac{L_2L_T}{L_2+L_T},$$

where

$$L_2 = \mu_0 2\pi R_c \frac{h}{l}$$

- inductance of the gap.

(6) 
$$L_{\tau} = \frac{\mu_0 \pi^2 R_0^2}{2l} \cdot \frac{\frac{R_c}{R_0}}{\left[1,46 + \ln \frac{\pi R_c}{4 (R_c - R)}\right] \frac{R_0}{l}} -$$

inductance of the ends of the solenoid.

In the calculations the gap inductance was calculated by formula (2), and the inductance of the ends - by formula (6).

an investigation of the solenoid-cylinder field on a model showed that the ratio of working current of the solenoid to the total current  $\frac{i_2}{i_2+i_1}$ , calculated with the help of formulas (2) and (6), in the case of the substitution of values  $\frac{R_c}{R_0} \approx 1.05$  and  $\frac{R_c}{l} \approx 0.5$ , corresponding to the real geometric dimensions of the solenoid, differed somewhat from experimental data. This difference is explained by the approximate nature of the formulas themselves and by the Very complex distribution of the field in the solenoid-cylinder system. For approximation of the experimental dependence  $\frac{i_2}{i_2+i_1}$  in the entire range of change of radius the factor  $\frac{R_0+R}{2R_c}$  is introduced into the formula.

The layout for substitution of the installation is shown in Figure 2. The inductance of scattering of the primary circuit  $L_1$ , the inductance of magnetization of the transformer  $L_\mu$ , the resistances of the primary circuit  $r_1$  and the solenoid  $r_2$  are considered constant, and their values are determined according to the oscillograms of discharge current of the bank on the solenoid.

The tested cylinders had an initial diameter of 95 mm and a length of 200 mm. Their other characteristics are given in Table 1.

The system of equations (1)-(4) was integrated on a computer together with the equations for the electrical circuit in Figure 2. The results of the calculation for a sample of type 1 with  $\Pi_0$ =120 kV are compared with experimental data in Figure 3. The satisfactory agreement of curves  $B_c$  and the radius of the cylinder  $R/R_0$  confirms the correctness of the selection of the parameters of the arrangement and the assumptions made under the given conditions. In the case of low initial voltages for heavy samples the experimental curves  $R/R_0$  lag behind the calculated, which is explained by the influence of the forces of resistance to deformation under these conditions. The curves of the internal field  $B_l$  differ strongly only in the case of deep compression, when the accepted description of the change in the parameters of the shell becomes insufficient. In the final stage the field  $B_l$  increases rapidly and the cylinder is slowed down.

Based on the maximum value of velocity the efficiency of acceleration  $\eta = \frac{mv_{\rm pair}^2}{CU_0^2}$  was determined. The calculated dependences of on the dimensionless parameter  $\beta = \frac{m\mu_0C^2U_0^2}{ml}$  for different samples are constructed in Figure 4. In the area  $\beta>0.2$  the calculated values agree satisfactorily with experimental, with smaller  $\beta$  an increase yields an excessive result.

In Table 2 the calculated values are given for the relative magnitudes of kinetic energy  $W_{\rm R}$ , electromagnetic energy  $W_{\rm SM}$ , thermal losses in resistances of the installation  $q_1+q_2$  and losses in the sample  $q_3$  by the moment of achievement of the maximum velocity for a sample of type 1.

With a lessening of ß there is an increase in the duration of compression and the share of thermal losses increases both in the cylinder and in the remaining resistors of the circuit. With 3<0.2 more than half of all the energy converts into heat. In this case the share of heat losses in the sample is not great - for aluminum it does not exceed 10 , for copper - 5 . Therefore the losses in the cylinder cannot have a significant influence on the conversion of energy during compression.

With an increase of  $\beta$  the share of thermal losses drops and the kinetic  $W_{k}$  and electromagnetic energy  $W_{k}$  are increased. At high values of  $\beta$  the latter reaches almost half of the initial stored energy  $W_{k}$ . During compression on this particular installation the inductance of the loop only doubles, and even in the absence of losses and an optimal value of  $\beta$  1 the efficiency does not exceed 0.5 [3], i.e., the greater part of the energy is preserved in the form of

electromagnetic. For an increase of efficiency it is necessary to lower the initial inductance of the installation being considered.

For an evaluation of the influence of the individual factors on the efficiency of acceleration the processes in the loop were calculated Without consideration of any other factors. For a sample of type 1 the following modes were considered: a)  $\alpha=0$ ; b)  $\Gamma_2=0$ ; c)  $\Gamma_3=0$ ; d)  $\Gamma_3=0$ , --=: e)  $\Gamma_3=0$ , --=: f)  $L_{\rm r}=L_{\rm r}=\infty$ ,  $\Gamma_1=\Gamma_2=\Gamma_3=0$ . In modes a and b the efficiency differs insignificantly from the previously obtained values, i.e., the losses in the solenoid and change in the resistance of the shell due to its heating up have little influence on the efficiency of acceleration.

The calculated dependences of \( \( \beta \) for modes c-f are depicted in Figure 4 by the broken lines. It is evident that both the penetration of the field and the presence of a pulsed transformer had an equal influence on the efficiency, although these two factors are more significant than the previous ones. A more noticeable influence is exerted by the flow of part of the solenoid current over its end surfaces, nonconsideration of this factor leads to almost a double overstating of efficiency (curve e). Therefore for an increase of effectiveness of acceleration the design of the solenoid has to be changed in such a way as to reduce the share of current which is flowing over the end surfaces.

Calculation in an idealized layout with disregard of losses and inductances  $L_{\tau}$  and  $L_{\mu}$  (curve f) gives results which differ still more from actual.

#### CONCLUSIONS

- 1. A calculated arrangement has been worked out for compression of thin-walled metallic shells in the field of a single-turn solenoid, taking into account penetration of the field into the shell, its heating up by vortex currents, redistribution of current over the surface of the solenoid, and the presence of a matching transformer in the discharge loop.
- 2. The accepted inertial model of deformation is applicable with 8>0.2. At smaller values the influence of the forces of resistance to deformation are significant.
- 3. The most important factors which determine the efficiency of acceleration in the arrangement which is considered are the active resistance and inductance of the primary circuit, and also the fact that part of the current of the solenoid flows on the ends of the

solenoid and do not participate in the creation of the working field.

Submitted by the TOE [expansion not verified] department

117 Nov 19691

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Figure 1. Solenoid with a deformable sample.

Key: (1) Solenoid; (2) Insulation; (3) Sample.

Table 1. Characteristics of test samples.

Key: (1) Type; (2) Material: (3) Thickness of wall,  $d_0$ , mm; (4) Mass, m', kg/m; (5) Active resistance,  $r_{30}$ , mohms; (6) Aluminum; (7) Copper.

Figure 2. Arrangement for substitution of discharge loop.

Figure 3. Compression of sample of type 1 with  $\Pi_0 = 120$  kV. Change in radius of shell:  $\Delta$ ,  $\Delta$  - experiment, 1 - calculated. Curves of magnetic induction: 2 - induction outside of the shell: 3 - induction inside of shell: a - experiment, b - calculated.

Key: (1) ms.

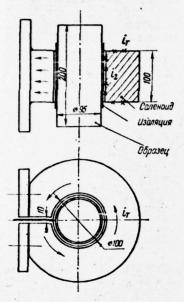
Table 2. Distribution of energy during compression of a cylinder.

Key: (1) ky; (2) kinetic; (3) electromagnetic.

Figure 4. Experimental and calculated values of efficiency of acceleration of a shell. Designation of experimental points: X - sample of type 1, O - sample of type 2,  $\bullet$  - sample of type 3,  $\Delta$  - sample of type 4. Calculated dependences are depicted by curves.

Key: (1) type 1; (2) type 2.

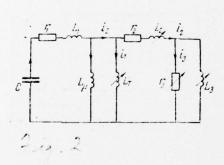
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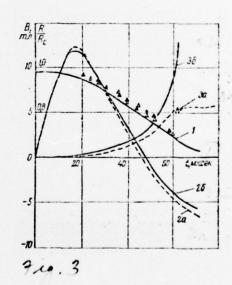


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Тип	Материал	Толщина стенки d <sub>0</sub> , мм	Macca m', кг/м	Активное сопротив- ление r <sub>30</sub> , мом
1	Алюминий	0,5	0,372	0,170
2	Медь	0,2	0,486	0,252
3	Медь	0,4	0,960	0,168
4	Медь	0,6	1,440	0,084

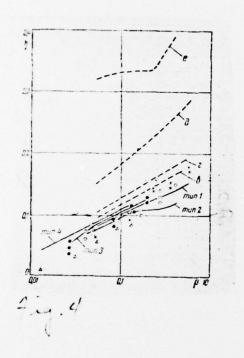
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Jable 2

U <sub>0</sub> , KB	β	W <sub>K</sub>	W <sub>o</sub>	$\frac{q_1+q_2}{W_0}$	
40	0,055	0,083	0,118	0,73	0.069
60	0,124	0,108	0,247	0.59	0,055
80	0,220	0,127	0,306	0,53	0,047
100	0,344	0,133	0,428	0,40	0.039
120	0,495	0,155	0,461	0,35	0.034



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